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# Effect of $\text{Pr}^{3+}/\text{Pr}^{4+}$ ratio on the oxygen ion transport and thermomechanical properties of the pyrochlore and fluorite phases in the $\text{ZrO}_2-\text{Pr}_2\text{O}_3$ system

A.V. Shlyakhtina <sup>a,\*</sup>, J.C.C. Abrantes <sup>b,c</sup>, E. Gomes <sup>c</sup>, A.N. Shchegolikhin <sup>d</sup>,  
G.A. Vorobieva <sup>a</sup>, K.I. Maslakov <sup>e</sup>, A.V. Knotko <sup>e</sup>, L.G. Shcherbakova <sup>a</sup>

<sup>a</sup> Semenov Institute of Chemical Physics, Russian Academy of Sciences, Moscow, 119991, Russia

<sup>b</sup> UIDM, ESTG, Instituto Politécnico de Viana do Castelo, Apartado 574, Viana do Castelo, 4901-348, Portugal

<sup>c</sup> Aveiro Institute of Materials—CICECO (DEMAC), University of Aveiro, Aveiro, 3810, Portugal

<sup>d</sup> Emanuel Institute of Biochemical Physics, Russian Academy of Sciences, ul. Kosygina 4, Moscow, 119991, Russia

<sup>e</sup> Faculty of Chemistry, Moscow State University, Leninskie gory 1, Moscow, 119991, Russia

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## ABSTRACT

This paper examines the effect of the  $\text{Pr}^{3+}/\text{Pr}^{4+}$  ratio on the mechanism of ionic and electronic transport in the  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ),  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlore phases and  $\text{Pr}_3\text{ZrO}_x$  with the fluorite structure and on the behavior of their thermal expansion coefficient (TEC). The solid solutions were prepared through coprecipitation followed by firing of the green compacts in air at a high temperature of 1550 °C for 4 h. The  $\text{Pr}^{3+}/\text{Pr}^{4+}$  ratio was shown to decrease in going from the  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ),  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlores to the  $\text{Pr}_3\text{ZrO}_x$  fluorite, leading to changes in the conductivity type from mixed (ionic–electronic) to electronic and in the color of the materials from beige to black and to an anomalous deviation of the TEC from linearity in fluorite  $\text{Pr}_3\text{ZrO}_x$ , i.e. at the highest  $\text{Pr}^{4+}$  content. According to impedance spectroscopy results,  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  with  $x = 0.15$  has purely oxide-ion conductivity ( $3 \times 10^{-3}$  S/cm at 1000 °C) in a wide range of oxygen partial pressures: from  $10^{-10}$  to  $10^2$  Pa. With increasing Pr content, p-type electronic conductivity becomes significant, reaching a maximum in fluorite  $\text{Pr}_3\text{ZrO}_x$ :  $\sim 0.5$  S/cm at 1000 °C. According to XPS data, all pyrochlore samples  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ),  $\text{Pr}_2\text{Zr}_2\text{O}_7$  and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) contain only  $\text{Pr}^{3+}$  at room temperature, whereas  $\text{Pr}_3\text{ZrO}_x$  contains both  $\text{Pr}^{3+}$  and  $\text{Pr}^{4+}$ . The considerable deviation of the TEC of  $\text{Pr}_3\text{ZrO}_x$  from linearity above 500 °C is due to partial reduction of  $\text{Pr}^{4+}$ . The reduction process  $\text{Pr}^{4+} + e^- \rightarrow \text{Pr}^{3+}$  followed by oxygen release in the range 500–1100 °C has been identified in  $\text{Pr}_3\text{ZrO}_x$  by thermal analysis and mass spectrometry in a He atmosphere.

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\* Corresponding author. Tel.: +7 495 9397950; fax: +7 499 2420253.

E-mail addresses: [annashl@inbox.ru](mailto:annashl@inbox.ru), [annash@chph.ras.ru](mailto:annash@chph.ras.ru) (A.V. Shlyakhtina).

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## Introduction

Many undoped and acceptor-doped  $\text{Ln}_2\text{M}_2\text{O}_7$  ( $\text{Ln} = \text{La-Lu}$ ;  $\text{M} = \text{Ti, Zr, Hf}$ ) pyrochlores are widely known oxygen vacancy conductors. Oxygen vacancy generation in these materials has been extensively discussed in the literature [1–10]. Their main potential application is solid electrolytes for SOFCs because they are close in oxide ion conductivity to the conventional  $\text{ZrO}_2$ -based solid electrolytes doped with 10–15 mol %  $\text{Y}_2\text{O}_3$  or  $\text{Sc}_2\text{O}_3$  [11]. Among the pyrochlore zirconates, the  $\text{Ln}_2\text{Zr}_2\text{O}_7$  ( $\text{Ln} = \text{Ce, Pr}$ ) zirconates, containing 3+/4+ variable-valence cations (Ce and Pr) are the least studied. The main reason for this is that during synthesis in air the  $\text{Ln}^{3+}$  in the  $\text{Ln}_2\text{Zr}_2\text{O}_7$  ( $\text{Ln} = \text{Ce, Pr}$ ) pyrochlores as a rule partially oxidizes to  $\text{Ln}^{4+}$  [12–15], which leads to coexistence of the  $\text{Ln}^{3+}$  and  $\text{Ln}^{4+}$  in the A site of  $\text{Ln}_2\text{Zr}_2\text{O}_7$  pyrochlores:



This process limits the use of these pyrochlores as solid electrolytes, but they can be studied as MIECs for SOFC electrodes.

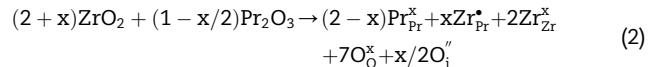
The Pr and Tb cations are the most stable in the pyrochlore structure among the known 3+/4+ variable-valence rare-earth cations [16]. In particular,  $\text{Tb}_2\text{Ti}_2\text{O}_7$  and  $\text{Tb}_2\text{Hf}_2\text{O}_7$  can be synthesized readily in air and the only compound in the  $\text{Tb}_2\text{O}_3-\text{ZrO}_2$  system is fluorite  $\text{Tb}_2\text{Zr}_2\text{O}_7$  ( $\text{TbZrO}_{4-\delta}$ ) [17,18].  $\text{Pr}_2\text{Zr}_2\text{O}_7$  can be prepared rather easily both by solid-state reaction and using solution techniques followed by high-temperature firing in air [15,19,20]. Undoped  $\text{Ce}_2\text{Zr}_2\text{O}_7$  can only be synthesized under reducing conditions, and subsequent exposure of this material to air leads to the oxidation of  $\text{Ce}^{3+}$  to  $\text{Ce}^{4+}$  [13,14]. Thus, because of the low potential of  $\text{Ce}^{3+} \rightarrow \text{Ce}^{4+}$  oxidation (1.44–1.7 V),  $\text{Ce}_2\text{Zr}_2\text{O}_7$  cannot be used as a SOFC material.

It should be emphasized that ionic and electronic transport processes in the  $\text{Pr}_2\text{O}_3-\text{ZrO}_2$  system have been the subject of a limited number of reports [15,19–22]. In connection with this, studies of  $\text{Pr}_x\text{Ce}_{1-x}\text{O}_{2-\delta}$  ( $x = 0, 0.01, 0.1, 0.2$ ) as potential SOFC cathodes [23–25] are of interest, where the oxide ion conductivity was measured as a function of oxygen partial pressure, the thermomechanical behavior of the materials was investigated, and anomalous thermal expansion was found at temperatures  $T > 500$ –600 °C in air, which was tentatively attributed to the reduction of  $\text{Pr}^{4+}$  to  $\text{Pr}^{3+}$  at these temperatures. This was accompanied by a considerable rise in electronic conductivity at elevated temperatures.

Because of this, we investigated not only the conductivity (as a function of oxygen partial pressure) but also the thermomechanical properties of pyrochlore-like  $\text{Pr}_2\text{O}_3-\text{ZrO}_2$  solid solutions in the rather narrow (~6 mol %) isomorphous miscibility range of  $\text{Pr}_{2+x}\text{Zr}_{2-x}\text{O}_{7+\delta}$  and those of a Pr-rich fluorite solid solution.

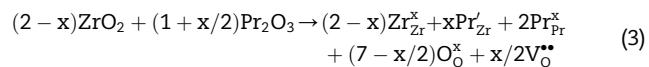
The following compositions were studied:

pyrochlore  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ), containing excess  $\text{Zr}^{4+}$  on the  $\text{Pr}^{3+}$  site, as a potential interstitial conductor, in which the formation of oxygen interstitials can be represented (in Kröger–Vink notation) by Eq. 2



the pyrochlore compound  $\text{Pr}_2\text{Zr}_2\text{O}_7$ ;

pyrochlore  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ), containing excess  $\text{Pr}^{3+}$  on the  $\text{Zr}^{4+}$  site, as a potential oxygen vacancy conductor, in which oxygen vacancy formation can be described by Eq. 3



and a  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 1$ ) Pr-rich fluorite solid solution.

## Experimental

Using coprecipitation followed by heat treatment at 1550 °C for 4 h, we prepared pyrochlore- and fluorite-like  $\text{PrZrO}$  solid solutions containing 30, 33.3, 35.5, and 60 mol %  $\text{Pr}_2\text{O}_3$  [20], which corresponds to the following compositions:  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ),  $\text{Pr}_2\text{Zr}_2\text{O}_7$ ,  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1, 1$ ).

The starting chemicals used were  $\text{PrCl}_3$  and  $\text{ZrOCl}_2 \cdot 8\text{H}_2\text{O}$  powders, which were dissolved in distilled water. Solution concentrations were determined gravimetrically. The concentrations of the chloride solutions were 0.09 M (Pr) and 1.085 M (Zr). All the  $\text{PrZrO}$  solid solutions were synthesized through reverse precipitation (pH 11.6–11.2), by adding titrated praseodymium chloride and zirconium chloride solutions to aqueous ammonia. After the formation of light green gel-like precipitates, they were aged at room temperature for 4 h. Next, the mother liquor was decanted and the rest was centrifuged. The precipitate was washed with warm water five times to remove  $\text{Cl}^-$  ions and then dried in air for 66 h at 75 °C, which allowed it to remain light green in color, typical of trivalent Pr. The development of a brown color during drying indicates the formation of  $\text{Pr}^{4+}$  centers.

The hydroxide precursors thus prepared were pressed at 259 (first composition) or 216 MPa (last three compositions) into pellets, which were then fired at 1550 °C for 4 h.

The density of the resultant samples was determined by measuring their mass and dimensions and ranged from 85 to 90% of their X-ray density [20]. All of the synthesized solid solutions were characterized by X-ray diffraction (XRD) on a DRON-3M (filtered  $\text{CuK}_\alpha$  radiation, step scan mode with a step of 0.05°, angular range  $2\theta = 10$ –100°, Rietveld refinement).

The oxidation state of the praseodymium in the solid solutions was determined by X-ray photoelectron spectroscopy (XPS) on a Kratos Axis Ultra DLD spectrometer using a monochromatic  $\text{Al K}\alpha$  X-ray source (1486.6 eV, 150 W). High-resolution spectra were acquired at 40 eV pass energy. The analysis area was about  $300 \times 700 \mu\text{m}$ . The binding energy scale of the spectrometer was preliminary calibrated using the following lines of standards (cleaned by ion sputtering): Au 4f<sub>5/2</sub> at 83.96 eV, Cu 2p<sub>3/2</sub> at 932.62 eV, and Ag 3d<sub>5/2</sub> at 368.21 eV. A Kratos charge neutralizer system was used. As the binding-energy-scale reference, we used the C 1s level (284.6 eV) arising from the carbon adsorbed on the sample surface.

Thermal analysis was carried out using a Netzsch STA 449C system in combination with an AEOLOS-32 mass

spectrometer between 25 and 1100 °C in helium atmosphere containing a small percentage of oxygen.

Thermomechanical analysis (TMA) curves were recorded in the range of 20–800 °C with the aid of a Perkin-Elmer TMA 7 analyzer equipped with a standard flat-tip probe. The samples in the form of pressed and prepolished disks (~2 mm thickness, ~6 mm dia.) were run at a heating rate of 5 K/min by using a TMA probe load of 100 mN. All the acquired TMA curves were processed using the NETZSCH-Proteus TA software package (v. 4.8.4). Only the TMA curves collected as the result of the second heating run were used for data mining. The physical  $\alpha$  curves specifying the linear thermal expansion coefficient (TEC) values of the sample at any given temperature (not shown) were automatically calculated with NETZSCH-Proteus TA by the following equation:  $\alpha_1(T) = 1/L_0 (dL/dT)$ , where  $L_0$  is the sample length (disk thickness) at the beginning of the TMA experiment (20 °C). Some TEC values taken at discrete temperatures are given in Table 3. The TEC transition onset temperatures were determined graphically from the abscissa intercepts of the tangents drawn on the two sides of the TMA peak (below and above the transition temperature).

Conductivity was measured in air between 300 and 750 °C and as a function of oxygen partial pressure (between 700 and 1000 °C) during reoxidation and after reduction with a mixture of 95% N<sub>2</sub> and 5% H<sub>2</sub>. A potentiometric oxygen sensor was used to monitor the oxygen partial pressure during the slow reoxidation process. Both pellet faces were coated with Pt paste (Engelhard) and the pellets were fired at 1000 °C for 30 min in order to obtain electrodes of lateral resistance < 1 Ω. The electrical measurements, both in a reducing atmosphere and in air, were made by impedance spectroscopy in the frequency range of 20 Hz–1 MHz, with a signal level between 100 and 250 mV (higher levels only at low temperature to avoid noise due to high resistance of the sample) using a Hewlett-Packard 4284A precision LCR bridge. The measurements of conductivity as a function of the oxygen partial pressure were performed only at high temperatures (700–1000 °C) due to oxygen sensor limitations. At these conditions the impedance spectra only present a single arc, attributed to the electrode reaction, or a single point over the x-axis, which corresponds to the total resistance of the sample.

## Results and discussion

### Structure of the $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$ ( $x = 0.15$ ), $Pr_2Zr_2O_7$ , and $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$ ( $x = 0.1$ ) pyrochlores and $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$ ( $x = 1$ ) fluorite studied by XRD: Rietveld refinement

Previously, Belov et al. [20] reported XRD data for the pyrochlore solid solutions under consideration. Here, we present XRD Rietveld refinement results for the same pyrochlore samples:  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ),  $Pr_2Zr_2O_7$ ,  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ) and  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 1$ ) fluorite (slow and fast cooling from 800 °C) (Fig. 1, a, b, c, d, e).

Tables 1 and 2 present Rietveld refinement results for all the pyrochlores. The percentages of cation antisite defects, antistructure pairs and occupancies of different oxygen

positions are indicated in Table 1. Our results (Tables 1 and 2) demonstrate that, like  $Nd_2Zr_2O_7$  [26,27],  $Pr_2Zr_2O_7$  has an ordered pyrochlore structure. This is obviously due to the rather large difference in ionic radius between  $Pr_{CN=8}^{3+}$  (1.126 Å) and  $Zr_{CN=6}^{4+}$  (0.72 Å). The structure of the  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 1$ ) Pr-rich solid solution (Fig. 1, d) was shown to be the most similar to the fluorite ( $CaF_2$ ) structure, with a unit-cell parameter of 5.41874(9) Å, which is close to that of undoped  $PrO_2$ : 5.392 Å (JCPDS PDF-2 24-1006). In what follows, we can write its formula as  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 1$ ) as  $Pr_3ZrO_x$ .

### XPS determination of the Pr valence state in the $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$ ( $x = 0.15$ ), $Pr_2Zr_2O_7$ , and $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$ ( $x = 0.1$ ) pyrochlores and $Pr_3ZrO_x$ fluorite

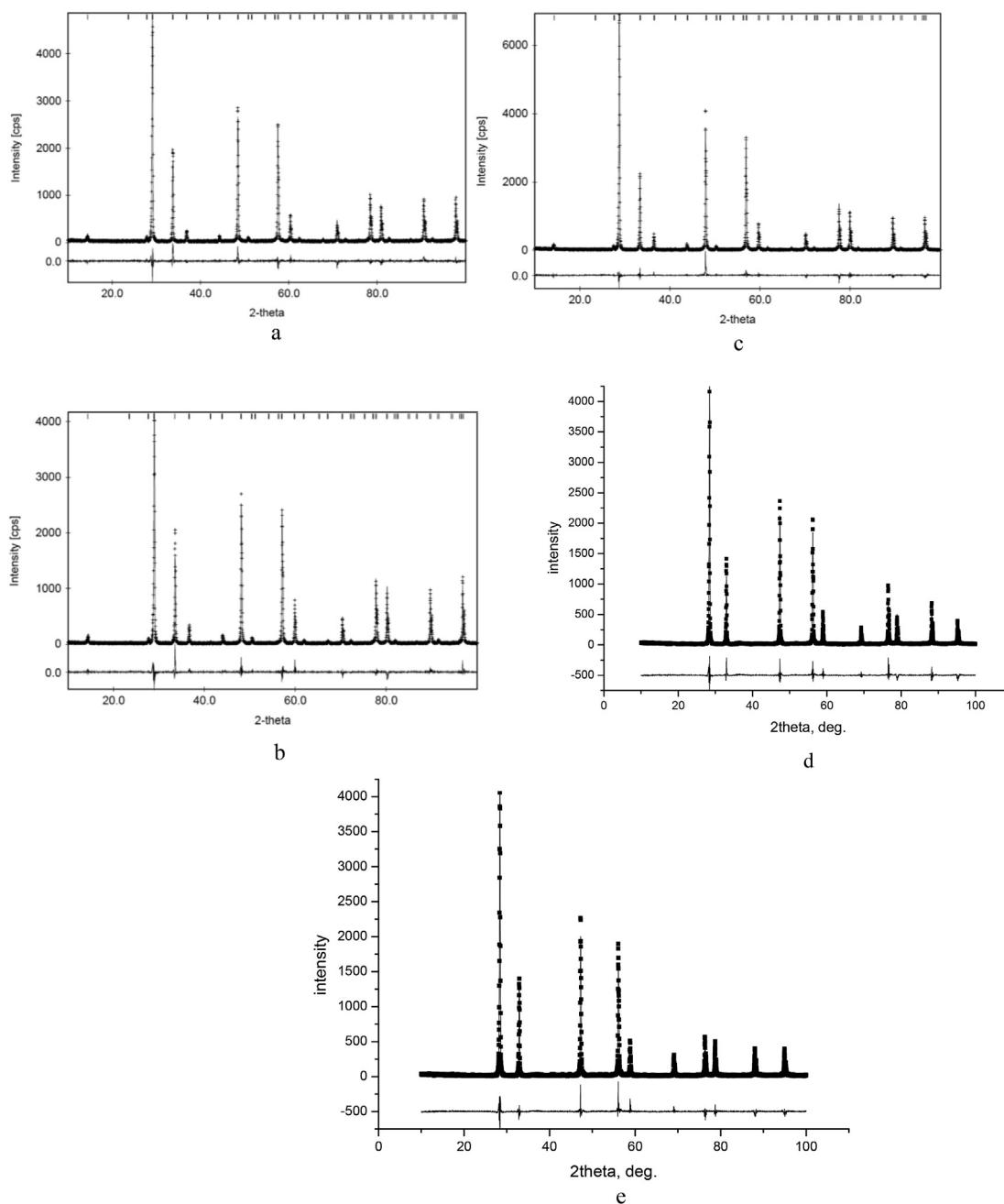
Arsentiev et al. [16] infer from phase diagram data for the  $Pr_2O_3$ – $ZrO_2$  system in air and vacuum [28–30] that, at large percentages of  $Pr_2O_3$  in  $mPr_2O_3$ – $nZrO_2$  mixtures (60 mol %  $Pr_2O_3$  in our case), thermal annealing in an oxidizing atmosphere increases the amount of  $Pr^{4+}$ . According to XRD data, the 60%  $Pr_2O_3$  – 40%  $ZrO_2$  ( $Pr_3ZrO_x$ ) material has the fluorite structure, whereas 30%  $Pr_2O_3$  – 70%  $ZrO_2$ , 33.3%  $Pr_2O_3$  – 67.7%  $ZrO_2$  and 35.5%  $Pr_2O_3$  – 64.5%  $ZrO_2$  have the pyrochlore structure.

The pyrochlore structure is known to be a fluorite-related superstructure with a higher degree of order. Fluorites have a loose structure, in which the oxidation state of cations may change, leading to oxygen release or absorption. Thus, the oxygen storage capacity of the fluorite structure exceeds that of the pyrochlore structure. It is for this reason that  $Pr^{4+}$  is more readily formed in fluorites, whereas the valence state of praseodymium in pyrochlores is typically 3+.

It seems likely that the  $Pr^{3+}$  cation in the cubic fluorite structure ( $CaF_2$ ) is less stable than in the pyrochlore structure ( $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ) and  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0, 0.1$ )) and that the Pr in  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  with  $x = 1$  ( $Pr_3ZrO_x$ ) is largely in its tetravalent state, so the formula of the  $Pr_3ZrO_x$  solid solution should be written as  $Pr_3ZrO_{8-\delta}$ .

To determine the  $Pr^{3+}/Pr^{4+}$  ratio we analyzed the XPS data for the solid solutions under investigation. The valence of the praseodymium (3+ or 4+) in the  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ),  $Pr_2Zr_2O_7$ , and  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ) pyrochlores and  $Pr_3ZrO_{8-\delta}$  fluorite solid solution synthesized through co-precipitation can be accurately determined by XPS. Hea et al. [31,32] and Sinev et al. [33] investigated the XPS spectra of  $Pr^{3+}$  and  $Pr^{4+}$  in the  $Pr_2O_3$ – $ZrO_2$  [33] and similar systems [31,32] for the powder samples. In this study, ceramic  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ),  $Pr_2Zr_2O_7$ ,  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ), and  $Pr_3ZrO_{8-\delta}$  samples were characterized by XPS.

Fig. 2 shows the room temperature Pr 3d XPS spectra of the  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ),  $Pr_2Zr_2O_7$ ,  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ), and  $Pr_3ZrO_{8-\delta}$  solid solutions. The chemical shift  $\Delta E_b$  of XPS lines is known to correlate with the effective charge on the atoms involved in bonding. Accordingly, the oxidation state of praseodymium is a quasi-linear function of the energy position of the Pr 3d level. This can be used to assess the chemical state of praseodymium in its compounds with oxygen.



**Fig. 1 – XRD Rietveld refinement profiles for the pyrochlore-like (a)  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ), (b)  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , (c)  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ), and (d) fluorite  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 1$ ) after slow cooling from 800°C, and (e) fluorite  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 1$ ) after rapid quenching (in liquid N<sub>2</sub>) from 800°C.**

**Table 1 – Compositions and XRD Rietveld refinement results.**

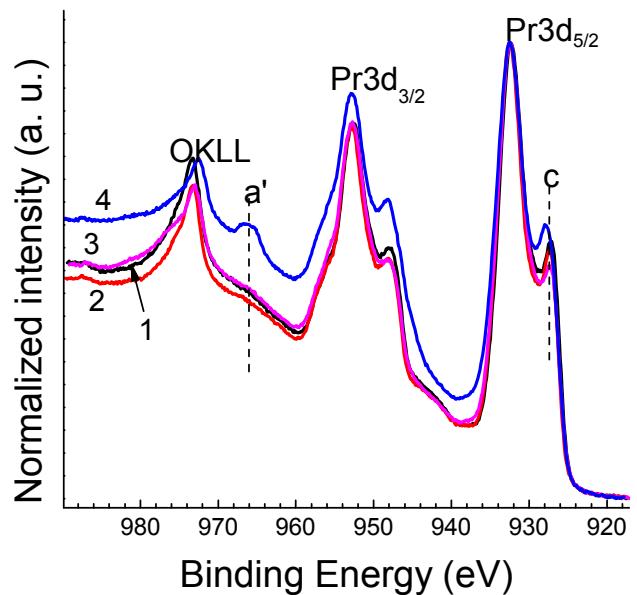
Mol. % $\text{Pr}_2\text{O}_3$	Formula	$\text{Zr}_{\text{Pr}}^* + \text{Pr}'_{\text{Zr}}$ antistructure pairs, %	$\text{Zr}_{\text{Pr}}^*$ antisite defects, %	$\text{Pr}'_{\text{Zr}}$ antisite defects, %	Interstitial oxygen in position 8b	Oxygen vacancy in position 48f	Relation between $\text{Pr}_{\text{Pr}}^x$ and $\text{Zr}_{\text{Zr}}^x$
30	$(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$ ( $x = 0.15$ )	3	10.5	3	0.08	0	$\text{Pr}_{\text{Pr}} < \text{Zr}_{\text{Zr}}$
33.3	$\text{Pr}_2\text{Zr}_2\text{O}_7$ ( $x = 0$ )	0	0	0	—	0	$\text{Pr}_{\text{Pr}} = \text{Zr}_{\text{Zr}}$
35.5	$\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$ ( $x = 0.096$ )	1.8	1.8	6.58	—	0.008	$\text{Pr}_{\text{Pr}} > \text{Zr}_{\text{Zr}}$

**Table 2 – Rietveld data for  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ),  $\text{Pr}_2\text{Zr}_2\text{O}_7$ ,  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) synthesized at 1550 °C in 4 h.**

Composition	Site	Occupancy	$x$	$y$	$z$	$R_{wp}$	$a, \text{\AA}$
						$R_p$	
						RR	
						Re	
						S	
						D	
						RI	
						RF, %	
$\text{Pr}_{1.85}\text{Zr}_{2.15}\text{O}_{7.08}$ (30% $\text{Pr}_2\text{O}_3$ )	$\text{Pr}_{\text{Pr}}$ (16d)	0.895(4)	0.625	0.625	0.625	15.03	10.6327(1)
	$\text{Zr}_{\text{Pr}}$ (16d)	0.105	0.625	0.625	0.625	11.19	
	$\text{Zr}_{\text{Zr}}$ (16c)	0.97	0.125	0.125	0.125	16.14	
	$\text{Pr}_{\text{Zr}}$ (16c)	0.03	0.125	0.125	0.125	11.13	
	O(1) (8a)	1	0.5	0.5	0.5	1.3503	
	O(2) (48f)	1	0.2143(6)	0	0	1.2178	
	O(3) (8b)	0.08	0.75	0.75	0.75	4.69	
						3.7	
$\text{Pr}_2\text{Zr}_2\text{O}_7$	$\text{Pr}_{\text{Pr}}$ (16d)	1	0.625	0.625	0.625	16.28	10.7175(1)
	$\text{Zr}_{\text{Pr}}$ (16d)	0	0.625	0.625	0.625	11.68	
	$\text{Zr}_{\text{Zr}}$ (16c)	1	0.125	0.125	0.125	15.13	
	$\text{Pr}_{\text{Zr}}$ (16c)	0	0.125	0.125	0.125	12.18	
	O(1) (8a)	1	0.5	0.5	0.5	1.3375	
	O(2) (48f)	1	0.2026(6)	0	0	1.2336	
						5.24	
						4.59	
$\text{Pr}_{2.092}\text{Zr}_{1.904}\text{O}_{6.952}$ (35.5% $\text{Pr}_2\text{O}_3$ )	$\text{Pr}_{\text{Pr}}$ (16d)	0.983(4)	0.625	0.625	0.625	13.96	10.7257(1)
	$\text{Zr}_{\text{Pr}}$ (16d)	0.018	0.625	0.625	0.625	10.04	
	$\text{Zr}_{\text{Zr}}$ (16c)	0.934	0.125	0.125	0.125	13.38	
	$\text{Pr}_{\text{Zr}}$ (16c)	0.066	0.125	0.125	0.125	10.75	
	O(1) (8a)	1	0.5	0.5	0.5	1.2982	
	O(2) (48f)	0.992	0.2050(6)	0	0	1.2588	
						5.3	
						4.16	

**Table 3 – Physical expansion coefficient  $\alpha$  (TEC) values for some discrete temperatures.**

T, °C	Samples			
	$(\text{Pr}_{2-x}\text{Zr}_x)$ $\text{Zr}_2\text{O}_{7+x/2}$ ( $x = 0.15$ )	$\text{Pr}_2\text{Zr}_2\text{O}_7$	$\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)$ $\text{O}_{7-x/2}$ ( $x = 0.1$ )	$\text{Pr}_3\text{ZrO}_x$
	Phys. $\alpha$ , 1/K x 10 <sup>-6</sup>	Phys. $\alpha$ , 1/K x 10 <sup>-6</sup>	Phys. $\alpha$ , 1/K x 10 <sup>-6</sup>	Phys. $\alpha$ , 1/K x 10 <sup>-6</sup>
50	7.954	8.005	9.446	7.639
100	9.324	11.188	9.448	10.340
150	9.943	10.778	9.672	10.102
200	10.283	11.513	10.270	10.443
250	10.512	10.679	10.500	9.913
300	9.539	10.652	10.828	8.795
350	10.543	10.696	10.264	9.587
400	10.996	11.148	9.889	8.512
450	11.608	11.894	11.254	6.129
500	12.026	12.414	11.192	10.208
550	12.201	12.788	11.827	21.397
600	15.104	14.805	12.515	22.978
650	15.752	15.225	13.669	21.080
700	16.796	17.814	15.385	21.913
750	16.644	18.387	17.348	22.689
800	25.118	17.135	13.305	28.843

**Fig. 2 – Pr 3d XPS spectra for (1)  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ), (2)  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , (3)  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ), and (4)  $\text{Pr}_3\text{ZrO}_x$  solid solutions at room temperature.**

The  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ),  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlore samples have similar spectra, in which line a', with a binding energy of ~966 eV, is missing (Fig. 2, curves 1–3). This shows that the praseodymium is almost completely in the valence state 3+ in these samples in accordance with [33]. In the spectrum of  $\text{Pr}_3\text{ZrO}_{8-\delta}$ , peak a' is clearly visible, and there is peak c with increased intensity, which indicates the presence of a significant amount of  $\text{Pr}^{4+}$  (Fig. 2, curve 4). At the same time, the relative intensity of peak a' is slightly lower than that in the spectrum of  $\text{PrO}_y$  [33]. This indicates that the praseodymium in  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 1$ ) is in a mixed (3+ and 4+) oxidation state and its formula should be written as  $\text{Pr}_3\text{ZrO}_x$ .

According to XPS analysis data, all the pyrochlore samples  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ),  $\text{Pr}_2\text{Zr}_2\text{O}_7$  and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) synthesized at 1550 °C in air contain only  $\text{Pr}^{3+}$  at room temperature, whereas  $\text{Pr}_3\text{ZrO}_x$  fluorite contains both  $\text{Pr}^{3+}$  and  $\text{Pr}^{4+}$ .

#### **The oxidation and reduction processes in the praseodymium pyrochlores and fluorite**

In the  $\text{Pr}_2\text{Zr}_2\text{O}_7$ ,  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$ , and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlore solid solution the oxidation process is possible at the higher temperatures:



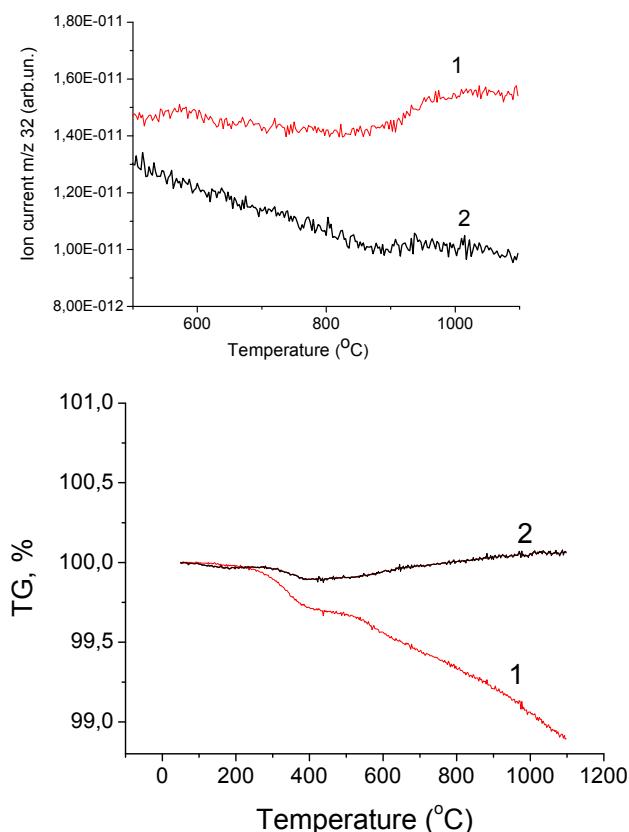
It starts at  $T \sim 270$  °C [15]. The rate of this process (Eq. (4)) is determined by the oxidation potential  $E^\circ\text{Pr}^{3+}/\text{Pr}^{4+} = 2.86\text{--}3.2$  V. This potential is significantly higher for the  $\text{Pr}^{3+}/\text{Pr}^{4+}$  pair than for  $\text{Ce}^{3+}/\text{Ce}^{4+}$  pair ( $E^\circ\text{Ce}^{3+}/\text{Ce}^{4+} = 1.44\text{--}1.7$  V). Indeed, in the  $\text{Ce}_2\text{Zr}_2\text{O}_7$  pyrochlore the oxidation process takes place at room temperature [14], while in  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0, 0.1$ ) this process does not occur at room temperature due to the high oxidation potential. The XPS data for the praseodymium pyrochlores (Fig. 2, curves 1–3) confirm this result (Section 3.2).

Above 270 °C, this process is enhanced. In Ref. [15] the retention of pyrochlore structure and oxidation of  $\text{Pr}^{3+}$  to  $\text{Pr}^{4+}$  in  $\text{Pr}_{2-x}\text{Ca}_x\text{Zr}_2\text{O}_7$  ( $x = 0, 0.075, 0.1$ ) in air at higher temperatures were inferred from thermogravimetry and in situ high temperature XRD data. In the low temperature region (270–500 °C), the oxidation process represented by Eq. (4) is possible for the  $\text{Pr}_3\text{ZrO}_x$  fluorite as well. However, it is known that  $\text{Pr}^{4+}$  start to reduce to  $\text{Pr}^{3+}$  at the temperatures  $T \geq 500$  °C, but nearly all of the  $\text{Pr}^{4+}$  ~80% is converted to  $\text{Pr}^{3+}$  above 1000 °C [23,34]. Consider now the possible reduction of  $\text{Pr}^{4+}$  in the  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlore and  $\text{Pr}_3\text{ZrO}_x$  fluorite solid solutions using TG data obtained in He.

According to literature data [23,34] the reduction process should take place at temperatures  $500 \leq T \leq 1100$  °C in  $\text{Pr}_3\text{ZrO}_x$  fluorite, but no or weak reduction occurs in the  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlore phase with a very small percent of  $\text{Pr}^{4+}$  on the  $\text{Pr}^{3+}$  sites of the pyrochlore structure [28]. Fig. 3 presents TG data of the  $\text{Pr}_3\text{ZrO}_x$  (Fig. 3, curve 1) and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) (Fig. 3, curve 2) in He in the temperature interval 25–1100 °C. The weight loss of  $\text{Pr}_3\text{ZrO}_x$  in He up to 500 °C is related to the physical water

release. The reduction of  $\text{Pr}^{4+}$  to  $\text{Pr}^{3+}$  in the  $\text{Pr}_3\text{ZrO}_x$  (Fig. 3, insert, curve 1) was accompanied by the formation of oxygen, as was evidenced by an increase in ion current at  $m/z = 32$  at  $T \sim 600$  °C and  $T > 800$  °C. This extent of process was very low in the  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlore at  $T > 800$  °C (Fig. 3, insert, curve 2). This result confirms the existence of  $\text{Pr}^{4+}$  in the  $\text{Pr}_3\text{ZrO}_x$ . In the  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlore praseodymium has predominantly 3+ oxidation state.

Michel et al. [28] determined the oxidation state of praseodymium in a fluorite phase of composition 60%  $\text{Pr}_2\text{O}_3$  – 40%  $\text{ZrO}_2$  ( $\text{Pr}_3\text{ZrO}_x$ ) after slow cooling from 800 °C and rapid quenching from the same temperature. The oxidation state of praseodymium was found to be 3.15 in the quenched sample and 3.34 in the slowly cooled sample. After slow cooling,  $\text{Pr}_3\text{ZrO}_x$  contained more  $\text{Pr}^{4+}$  and more oxygen. We have calculated the parameter of  $\text{Pr}_3\text{ZrO}_x$  fluorite after slow cooling from 800 °C and rapid quenching (in liquid N<sub>2</sub>) from the same temperature using Rietveld refinement (Fig. 1, d, e). The parameter of the cubic cell  $a$  was found to be 5.4297(1) Å in the quenched sample and 5.41874(9) Å in the slowly cooled sample. This result confirms the increasing of  $\text{Pr}^{3+}/\text{Pr}^{4+}$  ratio at high temperature (800 °C) and the decreasing of this ratio down to room temperature in  $\text{Pr}_3\text{ZrO}_x$  fluorite.



**Fig. 3 – TG data of (1)  $\text{Pr}_3\text{ZrO}_x$  and (2)  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) in He in the temperature interval 25–1100 °C. Insert: ion current for  $m/z = 32$  (oxygen) during heating of (1)  $\text{Pr}_3\text{ZrO}_x$  and (2)  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) in an inert atmosphere (He).**

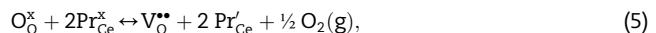
**Thermomechanical properties of the  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ),  $Pr_2Zr_2O_7$ , and  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ) pyrochlores and  $Pr_3ZrO_x$  fluorite**

**Fig. 4** and **Table 3** show thermomechanical data obtained in air for the potential ionic interstitial conductor  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  with  $x = 0.15$  (pyrochlore structure) (**Fig. 4** curve 1); the pure pyrochlore  $Pr_2Zr_2O_7$  (**Fig. 4** curve 2); the potential vacancy conductor  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  with  $x = 0.1$  (pyrochlore structure) (**Fig. 4** curve 3); and the Pr-rich fluorite solid solution  $Pr_3ZrO_x$  (**Fig. 4** curve 4). The curves can be divided into two groups. One group is formed by the curves of the pyrochlore materials, and the other, by the curve of the  $Pr_3ZrO_x$  fluorite phase. The TEC of the fluorite phase  $Pr_3ZrO_x$  considerably deviates from linearity above 500 °C (**Fig. 4**, curve 4). In the range 540–626 °C, the TEC of the pyrochlores also exhibits nonlinear behavior, but the deviation from linearity is markedly smaller (**Table 3**). In all cases, the TEC is on the order of  $(10\text{--}11.5) \times 10^{-6} \text{ K}^{-1}$  below the break. At higher temperatures, fluorite  $Pr_3ZrO_x$  has the largest TEC,  $22 \times 10^{-6} \text{ K}^{-1}$ , whereas the TEC of the pyrochlores is  $(15\text{--}18) \times 10^{-6} \text{ K}^{-1}$ .

Previously, similar nonlinearity was observed in the TEC of doped and undoped  $Dy_2Ti_2O_7$  pyrochlore at 700 °C, which was attributed to the antiferroelectric phase transition in the oxygen sublattice of pyrochlore-based solid solutions at this temperature [35]. Thus, oxygen mobility in both undoped and Ca-doped  $Ln_2Ti_2O_7$  pyrochlores changes above 700 °C [35]. A similar effect was observed earlier at ~500 °C in  $Sc_2O_3$ -doped  $ZrO_2$  with fluorite structure [36]. In the  $Sc_2O_3$  doped  $ZrO_2$  this effect is related to the ferroelastic  $\leftrightarrow$  ferroelectric phase transition from rhombohedral to the cubic phase [36]. We assume the phase transformation in our pyrochlore samples, which is associated with changes in the oxygen sublattice of  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ),  $Pr_2Zr_2O_7$ , and  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ) in the range 540–626 °C (**Table 3**). The fluorite-like phase – disordered pyrochlore phase transition near 800 °C

was observed recently by Payne et al. [37] for the neodymium zirconate  $Nd_2Zr_2O_7$ .

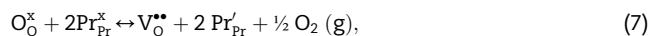
According to Rietveld data (Section 3.1), the structure of  $Pr_3ZrO_x$  is the most similar to the fluorite structure, with a unit-cell parameter of 5.41874(9) Å, which is close to that of  $PrO_{2-\delta}$ : 5.392 Å (JCPDS PDF-2 24-1006). At the room temperature  $Pr_3ZrO_x$  is deep black in color, which suggests high  $Pr^{4+}$  content, in agreement with the above XPS data (**Fig. 2**). In both pyrochlore and fluorite phases, the eight-coordinate ionic radius of  $Pr^{3+}$  is 1.126 Å and that of  $Pr^{4+}$  is considerably smaller: 0.96 Å [38]. What is then the cause of the marked deviation of the TEC of fluorite  $Pr_3ZrO_x$  from linearity above 500 °C? In a number of reports [23–25], the concept of chemical expansion was proposed for Pr-containing potential SOFC cathodes:  $Pr_xCe_{1-x}O_{2-\delta}$  ( $x = 0, 0.01, 0.1, 0.2$ ). Above 500 °C, the deviation of their TEC from linearity was found to increase with increasing Pr content. The oxygen loss from the  $Pr_xCe_{1-x}O_{2-\delta}$  ( $x = 0, 0.01, 0.1, 0.2$ ) lattice during high-temperature heat treatment or holding under reducing conditions follows the scheme [23].



where  $Pr_{Ce}^x - (Pr^{4+})$  and  $Pr'_{Ce} - (Pr^{3+})$  are Pr cations on the Ce site. At 700 °C and  $P_{O_2} > 10^{-18}$  atm, the electroneutrality condition has the form

$$[Pr'_{Ce}] \sim 2[V_O^{**}]. \quad (6)$$

Thus, the most likely cause of the chemical expansion of the  $Pr^{4+}$ -containing  $Pr_3ZrO_x$  sample under consideration is the increase in ionic radius in going from  $Pr^{4+}$  to  $Pr^{3+}$  during heating in air above 500 °C. The Kröger–Vink equations in this case have the form



where  $Pr_{Pr}^x = Pr^{4+}$  and  $Pr'_{Pr} = Pr^{3+}$ .

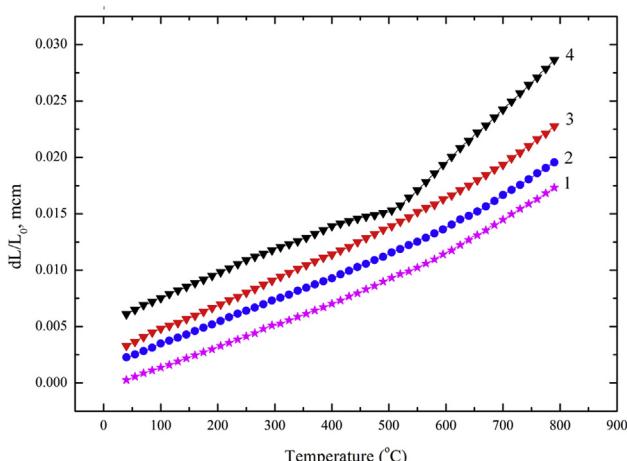
Similarly, at  $T > 500$  °C and  $P_{O_2} > 10^{-18}$  atm the electroneutrality condition has the form

$$[Pr'_{Pr}] \sim 2[V_O^{**}]. \quad (8)$$

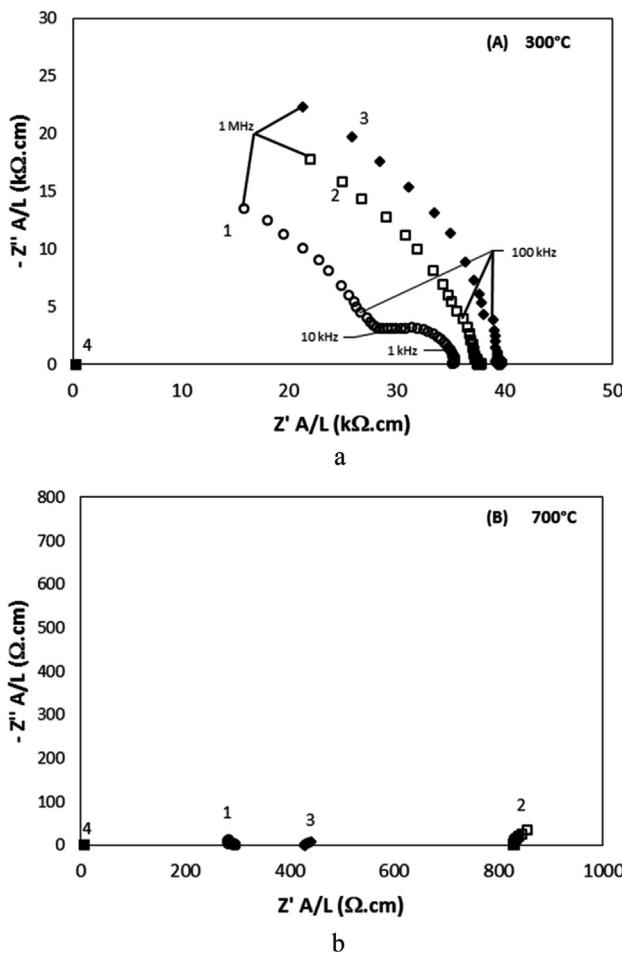
We believe that, during high-temperature annealing of  $Pr_3ZrO_x$  under oxidizing conditions in air, partial reduction of  $Pr^{4+}$  to  $Pr^{3+}$  is possible (**Fig. 3**) and that the expansion of the cubic cell due to the presence of the larger cation  $Pr^{3+}$  (Section 3.3) may be responsible for the deviation of the TEC from linearity above 500 °C (**Table 3**).

**Transport properties of the  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ),  $Pr_2Zr_2O_7$ , and  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ) pyrochlores and  $Pr_3ZrO_x$  fluorite**

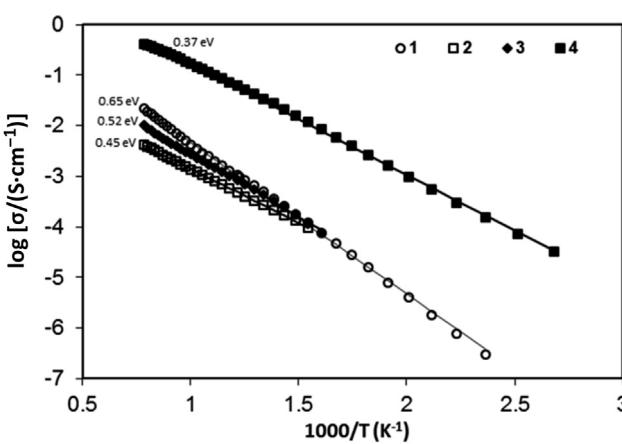
Transport properties were evaluated by impedance spectroscopy in air as functions of temperature and oxygen partial pressure at isothermal conditions. **Fig. 5** shows typical impedance spectra at 300 (**Fig. 5 a**) and 700 °C (**Fig. 5 b**). These spectra show that it is very easy to determine the total conductivity of each sample. However, deconvolution into bulk and grain boundary contributions is impossible, at least at high temperatures, ~700 °C. At low temperatures (**Fig. 5 a**), it is



**Fig. 4** – TMA curve for (1)  $(Pr_{2-x}Zr_x)Zr_2O_{7+x/2}$  ( $x = 0.15$ ), (2)  $Pr_2Zr_2O_7$ , (3)  $Pr_2(Zr_{2-x}Pr_x)O_{7-x/2}$  ( $x = 0.1$ ) and (4)  $Pr_3ZrO_x$  acquired during second heating of the samples from room temperature up to 800 °C. The curves are offset along the ordinate for clarity.



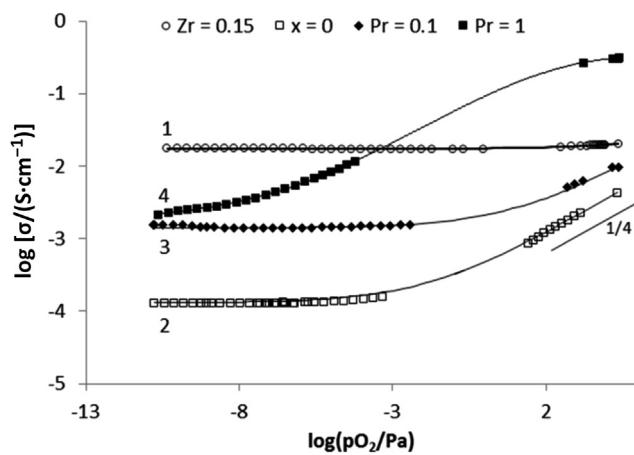
**Fig. 5 – Impedance spectra for (1)  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.15$ ), (2)  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , (3)  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-\frac{x}{2}}$  ( $x = 0.1$ ) and (4)  $\text{Pr}_3\text{ZrO}_x$  at (A) 300 °C and (B) 700 °C.**



**Fig. 6 – Arrhenius plot for (1)  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.15$ ), (2)  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , (3)  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-\frac{x}{2}}$  ( $x = 0.1$ ), and (4)  $\text{Pr}_3\text{ZrO}_x$  compositions in air. Activation energy values are written along each curve.**

possible to see a small semicircle related to the grain boundary contribution for  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.15$ ), but it was impossible to get this information to the other compositions, and so, total conductivity (bulk + grain boundary) was used to evaluate the electrical properties of these materials. The Arrhenius plot of total conductivity for  $\text{Pr}_3\text{ZrO}_x$  in air (Fig. 6 curve 4) demonstrates that this fluorite material has very high conductivity. The activation energies founded for each composition it will be discuss below.

Fig. 7 shows log-log plots of total conductivity vs. oxygen partial pressure for the  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.15$ ) interstitial oxide ion conductor (Fig. 7, curve 1),  $\text{Pr}_2\text{Zr}_2\text{O}_7$  ordered pyrochlore phase (Fig. 7, curve 2),  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-\frac{x}{2}}$  ( $x = 0.1$ ) oxygen vacancy conductor (Fig. 7, curve 3), and  $\text{Pr}_3\text{ZrO}_x$  Pr-rich fluorite solid solution (Fig. 7, curve 4) at 1000 °C. The highest contribution of the oxide ion conductivity was found in the  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.15$ ) interstitial conductor:  $3 \times 10^{-2}$  S/cm at 1000 °C (Fig. 7, curve 1) and  $6 \times 10^{-3}$  S/cm at 700 °C (Fig. 6, curve 1). The ordered pyrochlore phase  $\text{Pr}_2\text{Zr}_2\text{O}_7$  (Tables 1 and 2) had the lowest oxide ion conductivity contribution among the materials studied:  $\sim 1 \times 10^{-4}$  S/cm at 1000 °C (Fig. 7, curve 2). The  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-\frac{x}{2}}$  ( $x = 0.1$ ) oxygen vacancy conductor had intermediate oxide ion conductivity contribution:  $3 \times 10^{-3}$  S/cm at 1000 °C (Fig. 7, curve 3). A similar situation was observed previously for  $\text{Nd}_{2+x}\text{Zr}_{2+x}\text{O}_{7+\delta}$  solid solutions [26,27]: the highest conductivity was found in the  $(\text{Nd}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.2, 0.32, 0.39$ ) interstitial conductors, up to  $2.16 \times 10^{-3}$  S/cm at 700 °C, and the lowest, in the ordered pyrochlore phase  $\text{Nd}_2\text{Zr}_2\text{O}_7$ ,  $\sim 5 \times 10^{-5}$  S/cm at 700 °C. Note that the  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.15$ ) interstitial conductor was also found to have the widest range of predominantly oxide-ion conduction: from  $10^{-10}$  to  $10^2$  Pa (Fig. 7, curve 1). Under both reducing and mild oxidizing conditions,  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  with  $x = 0.15$  is a purely ionic conductor (Fig. 7, curve 1). In  $\text{Pr}_2\text{Zr}_2\text{O}_7$  and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-\frac{x}{2}}$  with  $x = 0.1$ , p-type conductivity prevails at 1000 °C and  $\text{P}_{\text{O}_2} > 10^{-5}$  Pa. At 1000 °C in air (for high oxygen partial pressures) all pyrochlores are mixed, ionic-electronic conductors in which electronic conduction prevails. Measurements preformed at 900, 800 and 700 °C,



**Fig. 7 – Electrical conductivity versus oxygen partial pressure for (1)  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+\frac{x}{2}}$  ( $x = 0.15$ ), (2)  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , (3)  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-\frac{x}{2}}$  ( $x = 0.1$ ), and (4)  $\text{Pr}_3\text{ZrO}_x$  compositions at 1000 °C.**

confirmed the same trend observed at 1000 °C, and due to YSZ sensor limitations, measurements below 700 °C were not performed.

The p-type conductivity of  $\text{Pr}_2\text{Zr}_2\text{O}_7$  (Fig. 7, curve 2) and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  with  $x = 0.1$  (Fig. 7, curve 3) at high oxygen partial pressures is controlled by intrinsic anti-Frenkel defects and by extrinsic Pr excess, respectively. The corresponding electroneutrality conditions are given by:

$$[\text{V}_\text{O}^{\bullet\bullet}] = [\text{O}_\text{i}^{\bullet}] \quad (9)$$

$$2[\text{V}_\text{O}^{\bullet\bullet}] = [\text{Pr}'_\text{Zr}] \quad (10)$$

These equations combined with the band–band transfer and with the atmosphere equilibrium, can be used to calculate the electronic hole concentration dependence as a function of the oxygen partial pressure:

$$0 \leftrightarrow e' + h' \quad (11)$$

$$K_e = np \quad (12)$$

$$\text{O}_\text{O}^x \leftrightarrow 1/2\text{O}_2 + \text{V}_\text{O}^{\bullet\bullet} + 2e' \quad (13)$$

$$K_{\text{ox}} = [\text{V}_\text{O}^{\bullet\bullet}] n^2 p \text{O}_2^{1/2} \quad (14)$$

$$p = K_e ([\text{V}_\text{O}^{\bullet\bullet}] / K_{\text{ox}})^{1/2} p \text{O}_2^{1/4} \quad (15)$$

As predict by Eqs. (9) and (10), the oxygen vacancy concentration are fixed, or by the anti-Frenkel defect equilibrium constant or by the non-stoichiometry, resulting in a  $1/4$  dependence of the p-type conductivity with the oxygen partial pressure, as observed in Fig. 7 (curves 2 and 3).

According to Table 1 and Eqs. (2) and (3), the interstitial conductor  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ) contains no oxygen vacancies but contains oxygen interstitials. The vacancy conductor  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) has partially filled oxygen vacancies and no interstitials. The interstitial oxygen ion conductor  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ) has a larger percentage of anti-structure pairs (3%) and higher oxygen ion conductivity. However, the anti-structure pairs do not affect the electroneutrality of the material, because the charge in each position is compensated and so, we do not expect significant effects on electrical conductivity, unless due to some changes in carrier mobility [39].

It was of particular interest to study fluorite ( $\text{Pr}_3\text{ZrO}_x$ ) [20], which had an anomalously high conductivity in air: 0.17 S/cm at 700 °C (0.5 S/cm at 1000 °C). The present results (Fig. 7, curve 4) demonstrate that in air this material is a p-type electronic conductor and that its ionic conductivity prevails at oxygen partial pressures below  $10^{-10}$  Pa, i.e. under highly reducing conditions. Its conductivity approaches the oxide ion conductivity of the  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) oxygen vacancy conductor:  $4 \times 10^{-3}$  S/cm at 1000 °C.

According to Rietveld data,  $\text{Pr}_3\text{ZrO}_x$  and  $\text{PrO}_{2-\delta}$  are close in unit-cell parameters. In fluorite  $\text{Pr}_3\text{ZrO}_x$ , a lot of praseodymium cations at room temperature are in 4+ valence state ( $\text{Pr}^{4+}$ ) (Section 3.2, Fig. 2 and Section 3.3). The co-existence of this two valent states can originate electron hopping between  $\text{Pr}^{3+}$  and  $\text{Pr}^{4+}$  positions. The shape of the oxygen partial pressure

dependence for  $\text{Pr}_3\text{ZrO}_x$  (Fig. 7, curve 4) with fluorite type structure, suggests that the conductivity reaches a maximum, in agreement with the small polaron mechanism for the conductivity, which should occur for  $\text{Pr}^{3+}/\text{Pr}^{4+} = 1$ . The oxidation state of praseodymium in that case should be 3.5 at the measurement temperature. For fluorite  $\text{Pr}_3\text{ZrO}_x$  the  $\text{Pr}^{3+}/\text{Pr}^{4+}$  ratio at high temperature ~800 °C is 3.15 [28]. Then it is possible only weak small polaron contribution to the conductivity of fluorite  $\text{Pr}_3\text{ZrO}_x$ . This type of conductivity was also found by Bishop et al. [34] for Pr-doped cerium oxide, also with the fluorite structure.

The stoichiometric composition  $\text{Pr}_2\text{Zr}_2\text{O}_7$  (Fig. 7, curve 2) also shows an evident increase of conductivity at high oxygen partial pressures. However, XPS measurements only reveal the presence of  $\text{Pr}^{3+}$ , without any traces of  $\text{Pr}^{4+}$ , at room temperature, and it is not expected a transition from  $\text{Pr}^{3+}$  to  $\text{Pr}^{4+}$  at the measurement temperature (1000 °C). So, it is not realistic to consider hoping mechanism for the electronic conductivity founded in these compositions in oxidizing conditions. Note that in the fluorite Pr-doped cerium oxide, the  $\text{Pr}^{3+}$  ion is at  $\text{Ce}^{4+}$  position, with trend to oxidize, and otherwise, in the pyrochlore  $\text{Pr}_2\text{Zr}_2\text{O}_7$ , the  $\text{Pr}^{3+}$  is in his natural position. Consequently, we suggest that the p-type conductivity is due to the band–band transfer, in agreement with Eqs. (11) and (12), resulting in a  $1/4$  dependence with the oxygen partial pressure, as predict by Eq. (15).

Based on XPS results, similar conclusions can be made for  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) (Fig. 7, curve 3), i.e., the onset on the electronic conductivity at high oxygen partial pressures is due the p-type conductivity in the valence band.

For  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  with  $x = 0.15$  (Fig. 7, curve 1) the p-type and the ionic conductivities, for high oxygen partial pressures, have the same order of magnitude and so, in this conditions, we have a mixed conductor.

The activation energies obtained in air, Fig. 6, are in agreement with the conduction mechanism founded. Taking into account the ionic conductivity for each composition (low oxygen partial pressures conductivities) between 700 and 1000 °C, we get an activation energy of about 1 eV for all pyrochlores and 1.5 eV for the fluorite composition. Differences between activations energies in Fig. 6 are related with the mixed nature of the conduction of these materials. The activation energy increases with the increase of the ionic component weight.

## Conclusions

We have investigated the effect of  $\text{Pr}^{3+}/\text{Pr}^{4+}$  ratio on the oxygen ion transport and thermomechanical properties of the solid solutions in the  $\text{ZrO}_2 - \text{Pr}_2\text{O}_3$  binary oxide system. The solid solutions were prepared through coprecipitation followed by pressing and firing of the green compacts in air at 1550 °C. The  $\text{Pr}^{3+}/\text{Pr}^{4+}$  ratio was shown to decrease across the above series in going from pyrochlores to fluorite, leading to changes in the conductivity type and color of the solid solutions and the behavior of their TEC. In particular, the  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  ( $x = 0.15$ ) pyrochlore solid solution is a purely interstitial oxide ion conductor ( $3 \times 10^{-2}$  S/cm at 1000 °C) in a wide range of oxygen partial pressures: from  $10^{-10}$  to  $10^2$  Pa.

However in air this material is mixed, ionic–electronic conductor. In the  $\text{Pr}_2\text{Zr}_2\text{O}_7$  and  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) pyrochlores, p-type conduction prevails at 1000 °C and  $\text{P}_{\text{O}_2} > 10^{-5}$  Pa, i.e. in air these materials are mixed, ionic–electronic conductors in which hole conduction prevails. For  $\text{P}_{\text{O}_2} < 10^{-5}$  Pa, the 1000 °C oxide ion conductivity of pyrochlore  $\text{Pr}_2\text{Zr}_2\text{O}_7$  and that of the pyrochlore  $\text{Pr}_2(\text{Zr}_{2-x}\text{Pr}_x)\text{O}_{7-x/2}$  ( $x = 0.1$ ) oxygen vacancy conductor are  $1 \times 10^{-4}$  and  $3 \times 10^{-3}$  S/cm, respectively, and are lower than that of  $(\text{Pr}_{2-x}\text{Zr}_x)\text{Zr}_2\text{O}_{7+x/2}$  with  $x = 0.15$ . Fluorite  $\text{Pr}_3\text{ZrO}_x$  is a p-type electronic conductor with a 1000 °C conductivity of 0.5 S/cm. However the weak small polaron contribution may exist in this fluorite. The considerable deviation of the TEC of  $\text{Pr}_3\text{ZrO}_x$  fluorite from linearity above 500 °C is due to partial reduction of  $\text{Pr}^{4+}$ , which leads to an increase in the unit-cell parameter and, hence, in the dimensions of the sample. The reduction of  $\text{Pr}^{4+}$  to  $\text{Pr}^{3+}$  in the  $\text{Pr}_3\text{ZrO}_x$  fluorite above 500 °C has been identified using TG and mass spectrometry in a He atmosphere.

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